

Original Problem	Steady-state Problem	Transient Problem
$\frac{\partial^2 u}{\partial x^2} = \frac{1}{k} \frac{\partial u}{\partial t}, \quad 0 < x < a, 0 < t$ $u(0, t) = T_0, u(a, t) = 0, \quad 0 < t$ $u(x, 0) = T_0 x / a, \quad 0 < x < a$	$v'' = 0, 0 < x < a$ $v(0) = T_0, v(a) = 0$ <b>S:</b> $v(x) = T_0(1 - x/a)$	
$\frac{\partial^2 u}{\partial x^2} + H = \frac{1}{k} \frac{\partial u}{\partial t}, \quad 0 < x < a, 0 < t$ $u(0, t) = 0, u(a, t) = U_0, \quad 0 < t$ $u(x, 0) = U_0, 0 < x < a$	$v'' + H = 0, 0 < x < a$ $v(0) = 0, v(a) = U_0$ <b>S:</b> $v(x) = U_0 x/a + H(ax - x^2)/2$	
$\frac{\partial^2 u}{\partial x^2} - \gamma^2 u = \frac{1}{k} \frac{\partial u}{\partial t}, \quad 0 < x < a, 0 < t$ $u(0, t) = U_0, u(a, t) = U_1, \quad 0 < t$ $u(x, 0) = U_0 \sin(\pi x/2a), 0 < x < a$	$v'' - \gamma^2 v = 0, 0 < x < a$ $v(0) = U_0, v(a) = U_1$ <b>S:</b> $v(x) = U_0 \cosh(\gamma x) + (U_1 - U_0 \cosh(\gamma a)) \sinh(\gamma x) / \sinh(\gamma a)$	
$\frac{\partial^2 u}{\partial x^2} = \frac{1}{k} \frac{\partial u}{\partial t}, \quad 0 < x < a, 0 < t$ $\frac{\partial u}{\partial x}(0, t) = 0, \frac{\partial u}{\partial x}(a, t) = 0, \quad 0 < t$ $u(x, 0) = Tx/a, \quad 0 < x < a$	$v'' = 0, 0 < x < a$ $v(0)' = 0, v'(a) = 0$ <b>S:</b> $v(x) = \text{const (undetermined)}$	
$\frac{\partial^2 u}{\partial x^2} = \frac{1}{k} \frac{\partial u}{\partial t}, \quad 0 < x < L, 0 < t$ $u(0, t) = T_0, \frac{\partial u}{\partial x}(L, t) = 0, \quad 0 < t$ $u(x, 0) = T_0 \quad 0 < x < L$	$v'' = 0, 0 < x < L$ $v(0) = T_0, v'(L) = 0$ <b>S:</b> $v(x) = T_0$	
$\frac{\partial^2 u}{\partial x^2} = -\gamma^2(T - u) + \frac{1}{k} \frac{\partial u}{\partial t}, \quad 0 < x < a, 0 < t$ $\frac{\partial u}{\partial x}(0, t) = 0, u(a, t) = U_0, \quad 0 < t$ $u(x, 0) = -U_0 \cos(\pi x/a), 0 < x < a$	$v'' = -\gamma^2(T - v), 0 < x < a$ $v'(0) = 0, v(a) = U_0$ <b>S:</b> $v(x) = T + (U_0 - T) \frac{\cosh(\gamma x)}{\cosh(\gamma a)}$	