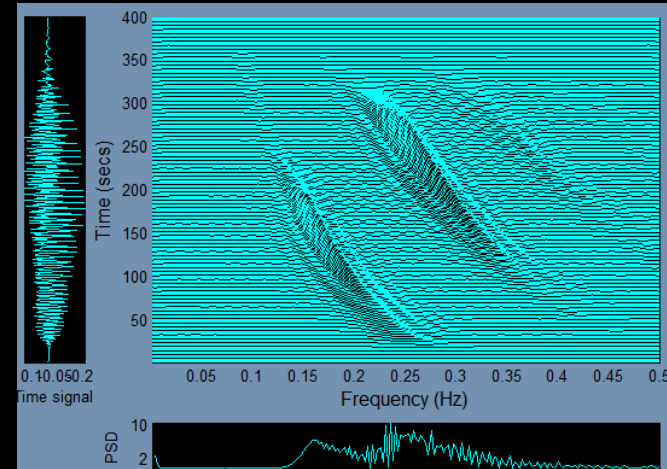
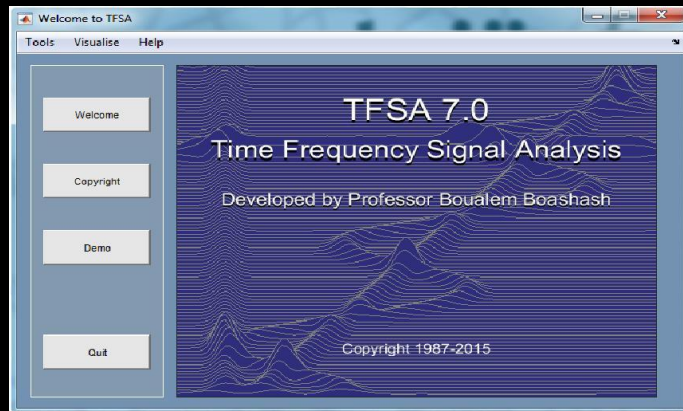


PART B:

TFSA 7.0 Tutorial



Prof. B. Boashash

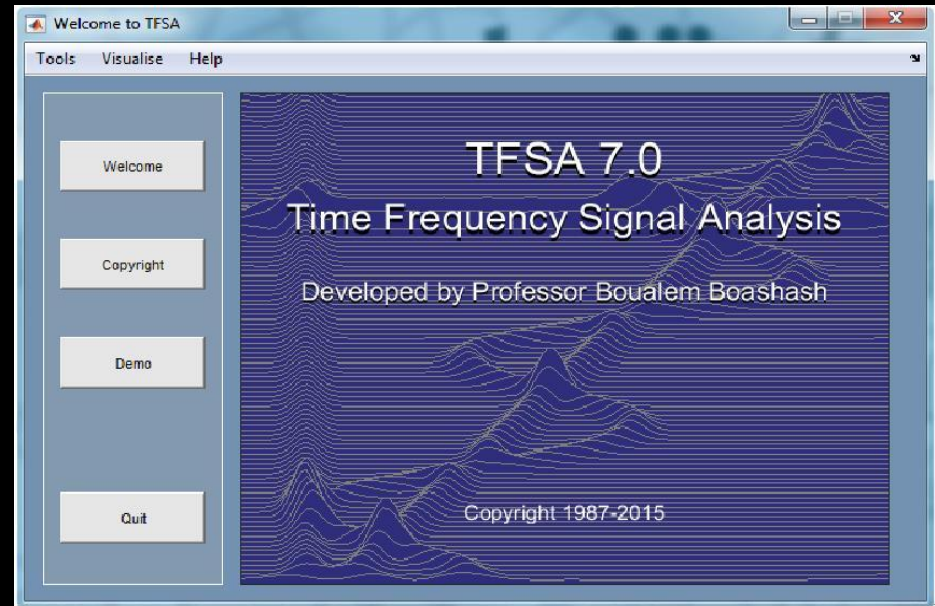
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^b *College of Engineering, Qatar University, Doha, Qatar*

^c *formerly Director, SPRC, Queensland University of Technology, Brisbane, Australia*

TFSA Toolbox

- Time-Frequency Signal Analysis Matlab® Toolbox
- Developed by Prof. Boualem Boashash
- Graphical User Interface
- MEX formatting
- UNIX and WINDOWS
- 20 years of development
- Additional information can be found at:



<http://www.time-frequency.net/downloads.html>

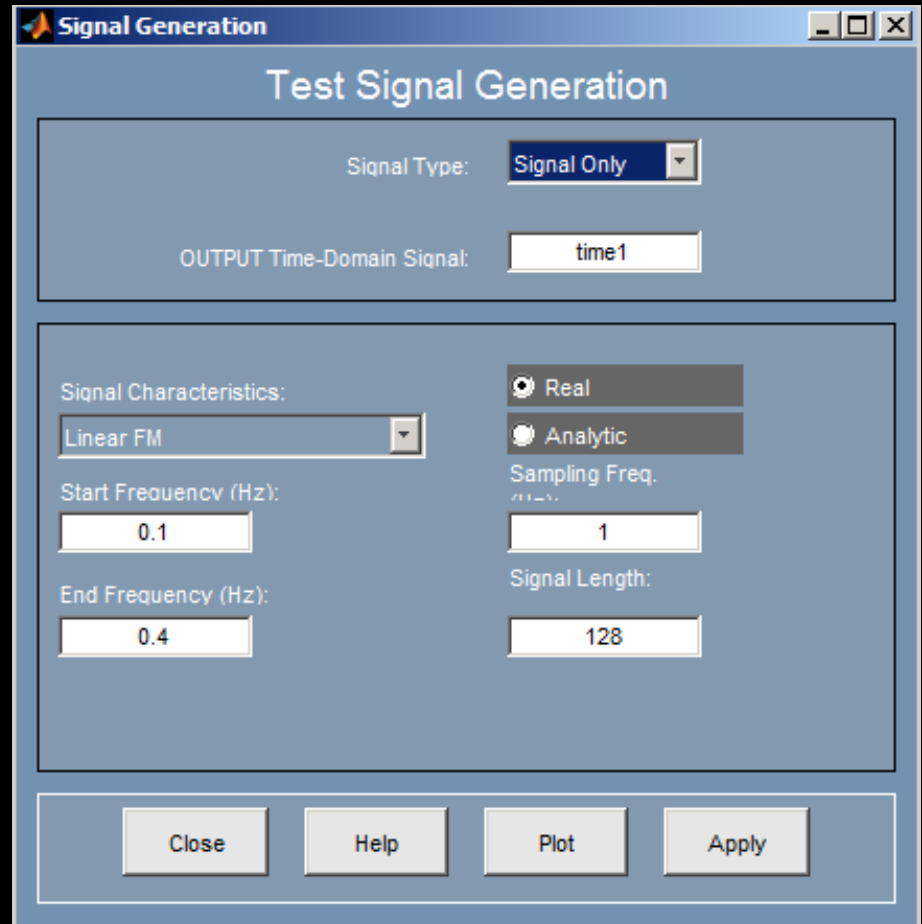
Content

- The toolbox addresses the issues of
 - Nonstationary signal generation
 - Analytic signal generation
 - Quadratic time-frequency distributions
 - Instantaneous frequency estimation
 - Time-frequency signal synthesis

Signal Generation

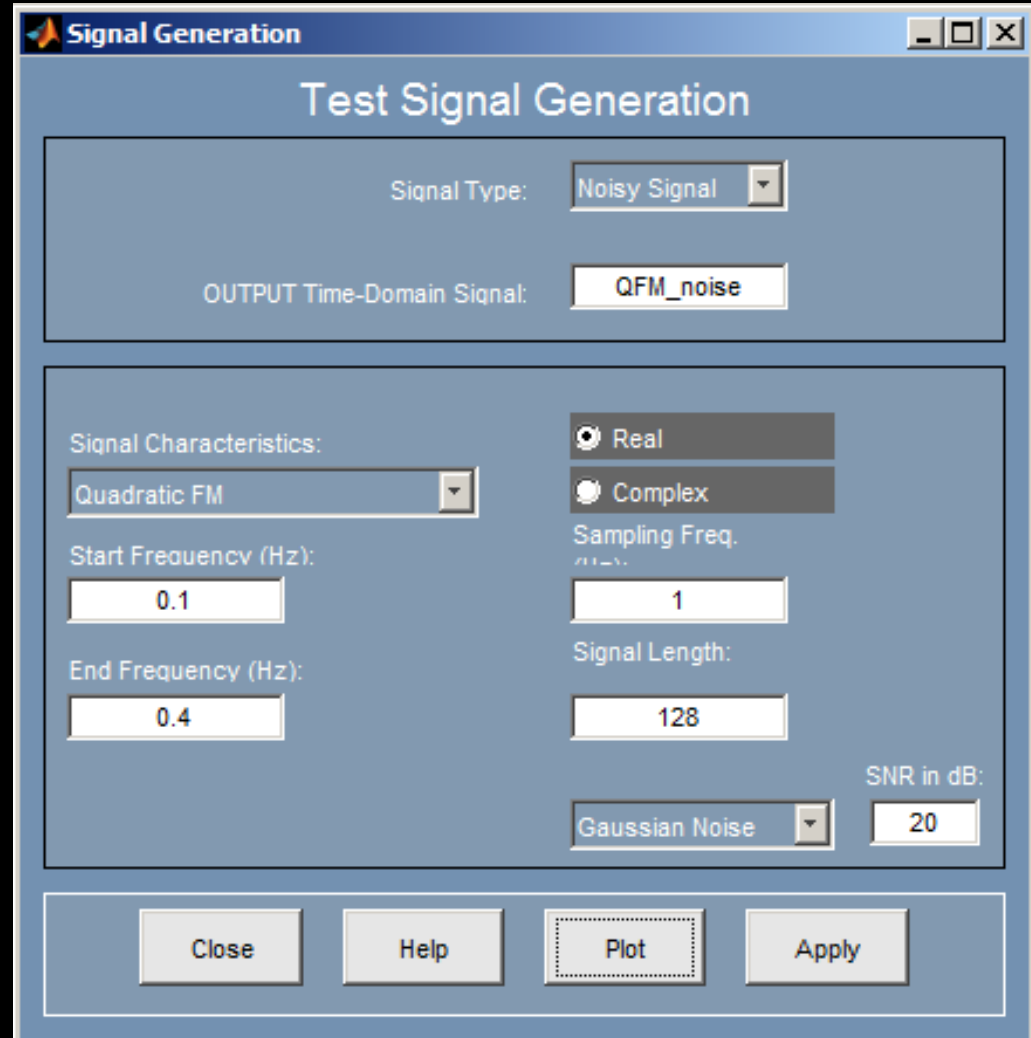
- Types of signal generated

- Linear FM
- Quadratic FM
- Cubic FM
- Hyperbolic FM
- Sinusoidal FM
- Stepped FM
- Noise
 - Gaussian
 - Uniform
- Signal + Noise
 - SNR
- Real or Complex




Example: - Quadratic FM + noise

Generate a real quadratic FM signal (length = 128 samples) that ranges from 0.1 to 0.4 Hz (normalised) with AWGN (SNR = 20dB).



The image shows a software window titled "Signal Generation" with a subtitle "Test Signal Generation". It contains several input fields and buttons for configuring a signal. The "Signal Type" is set to "Noisy Signal". The "OUTPUT Time-Domain Signal" is "QFM_noise". Under "Signal Characteristics", "Quadratic FM" is selected. The "Start Frequency (Hz)" is 0.1 and the "End Frequency (Hz)" is 0.4. The "Signal Characteristics" section also has radio buttons for "Real" (selected) and "Complex". The "Sampling Freq." is 1 and the "Signal Length" is 128. The "SNR in dB" is 20, with "Gaussian Noise" selected. At the bottom are buttons for "Close", "Help", "Plot", and "Apply".

| Parameter | Value |
|---------------------------------------|----------------|
| Signal Type | Noisy Signal |
| OUTPUT Time-Domain Signal | QFM_noise |
| Signal Characteristics | Quadratic FM |
| Start Frequency (Hz) | 0.1 |
| End Frequency (Hz) | 0.4 |
| Signal Characteristics (Real/Complex) | Real |
| Sampling Freq. | 1 |
| Signal Length | 128 |
| SNR in dB | 20 |
| Noise Type | Gaussian Noise |

 **Signal Generation** [-] [] [X]

Test Signal Generation

Signal Type: Noisy Signal ▾

OUTPUT Time-Domain Signal: QFM_noise

Signal Characteristics: Quadratic FM ▾

Start Frequency (Hz): 0.1

End Frequency (Hz): 0.4

☒ Real

☐ Complex

Sampling Freq. (Hz): 1

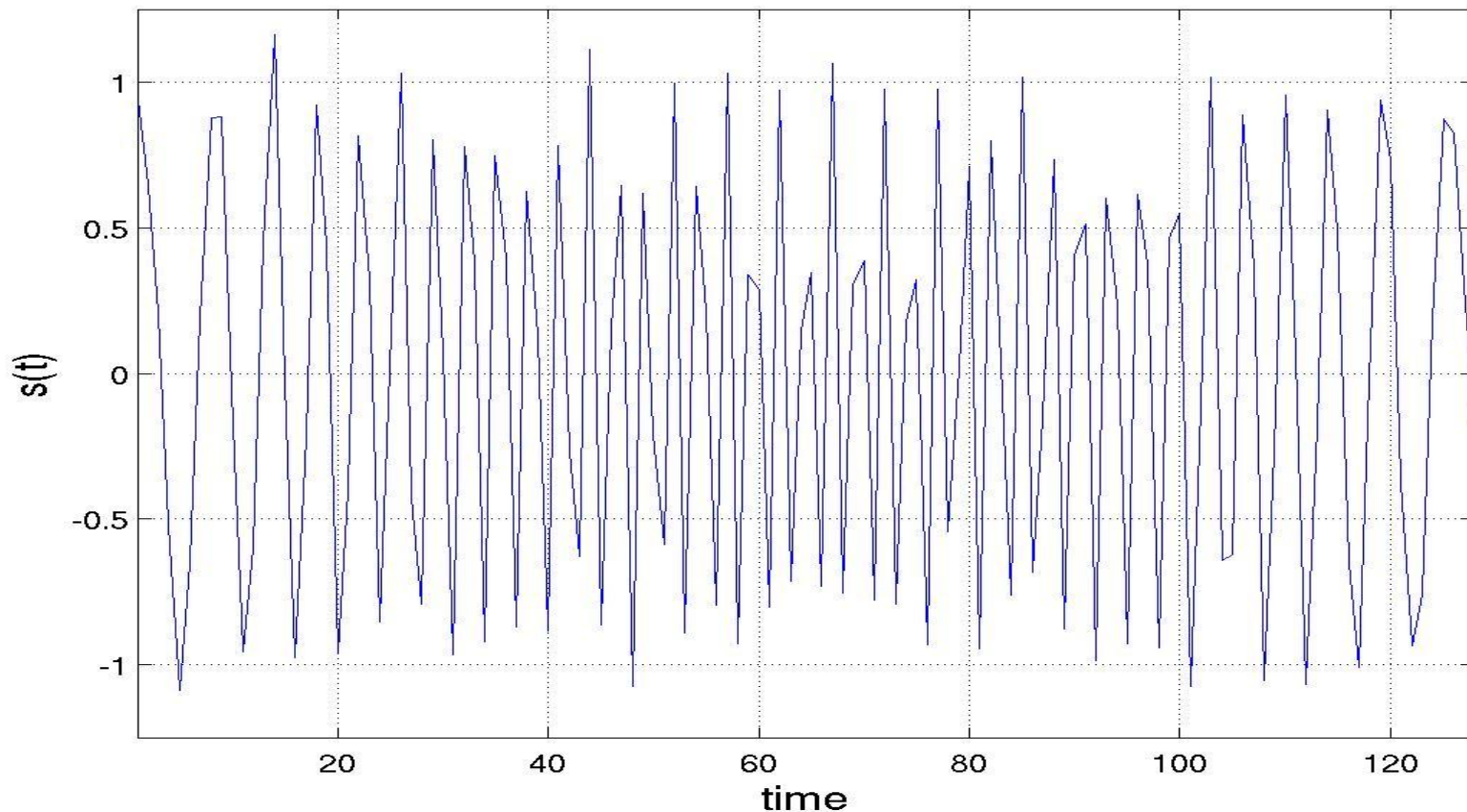
Signal Length: 128

SNR in dB: Gaussian Noise ▾ 20

Close Help Plot Apply

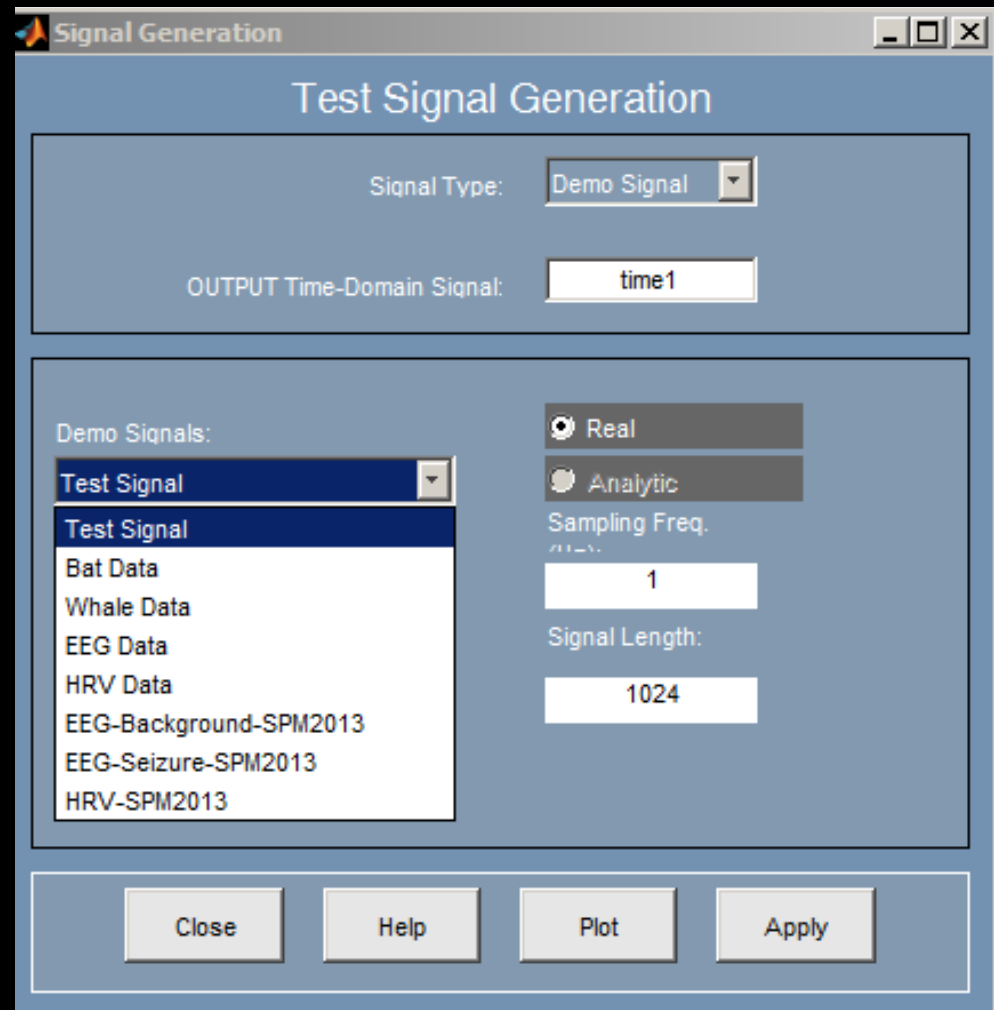
Generated Signal

```
>> plot(QFM_noise)
```



Demo Signals

- Database of real world nonstationary example signals
 - Whale Song
 - Bat
 - Newborn EEG
 - HRV
 - Arbitrary test signal



Signal Generation

Test Signal Generation

Signal Type: Demo Signal

OUTPUT Time-Domain Signal: bat1

Demo Signals:

Bat Data

☒ Real

☐ Analytic

Sampling Freq.
(Hz):

142000

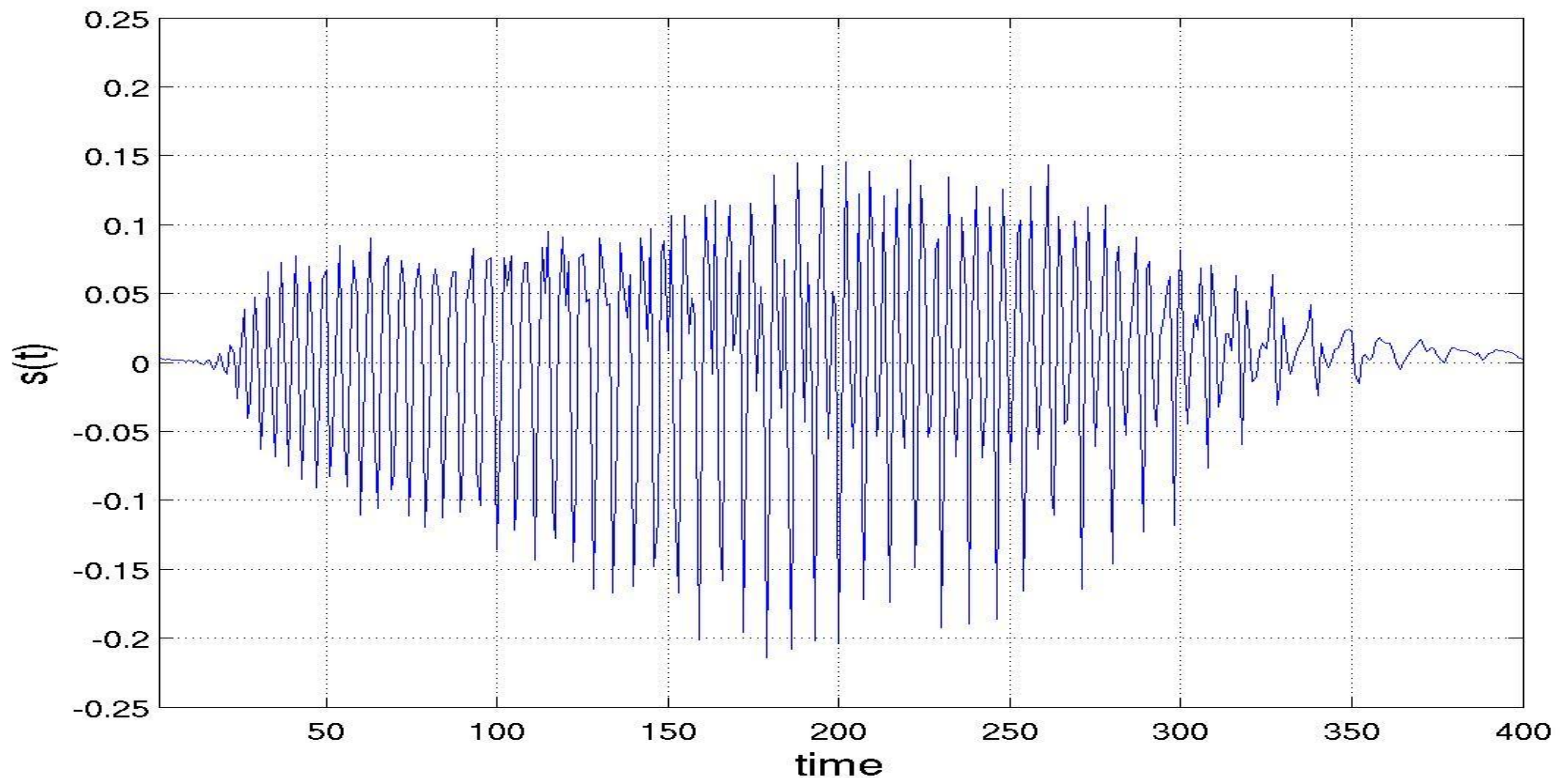
Signal Length:

400

Close Help Plot Apply

Example

- Bat echolocation >> plot(bat1)



Analytic Signal Generation

- The analytic signal is an important fundamental concept in time-frequency signal analysis (chapter 1)

$$z(t) = s(t) + j \left[s(t) * \frac{1}{\pi t} \right]$$

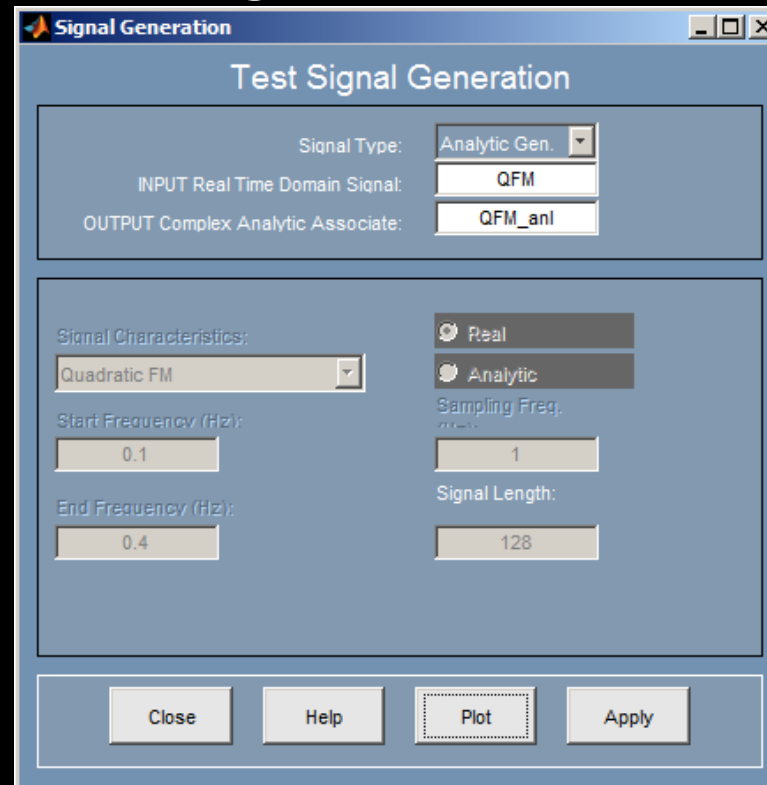
- In polar form

$$z(t) = a(t) e^{j\phi(t)}$$

- TFSA generates the analytic signal using a frequency domain method.

Analytic Signal Example

- Generate the analytic signal of the quadratic FM signal



Signal Generation

Test Signal Generation

Signal Type: Analytic Gen. ▾

INPUT Real Time Domain Signal: QFM

OUTPUT Complex Analytic Associate: QFM_anl

Signal Characteristics:
Quadratic FM ▾

Start Frequency (Hz): 0.1

End Frequency (Hz): 0.4

☒ Real
☐ Analytic

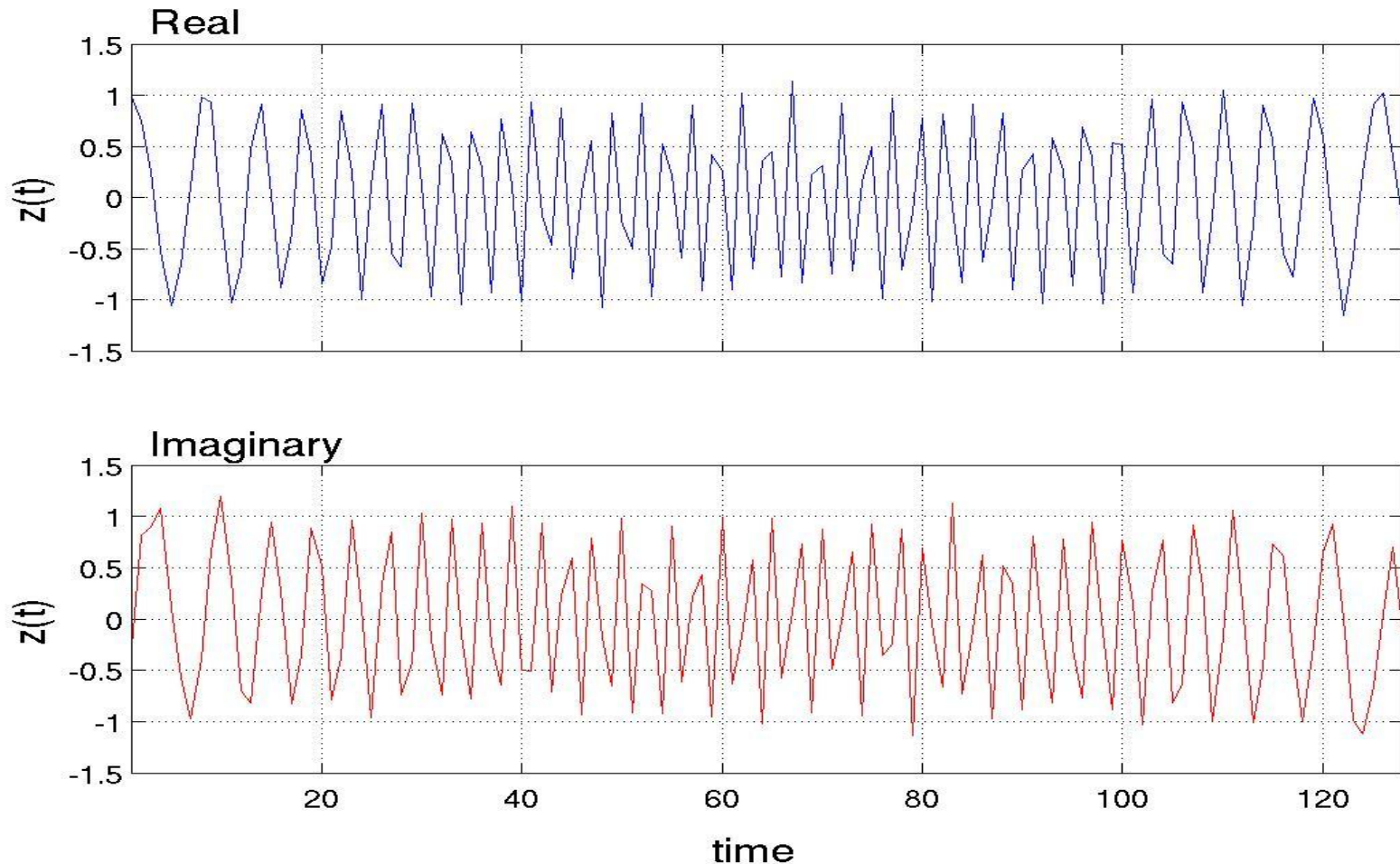
Sampling Freq. 1

Signal Length: 128

Close Help Plot Apply

Analytic Signal Example

```
>> plot(real(QFM_anl)); hold; plot(imag(QFM_anl,'r'))
```



IF estimation

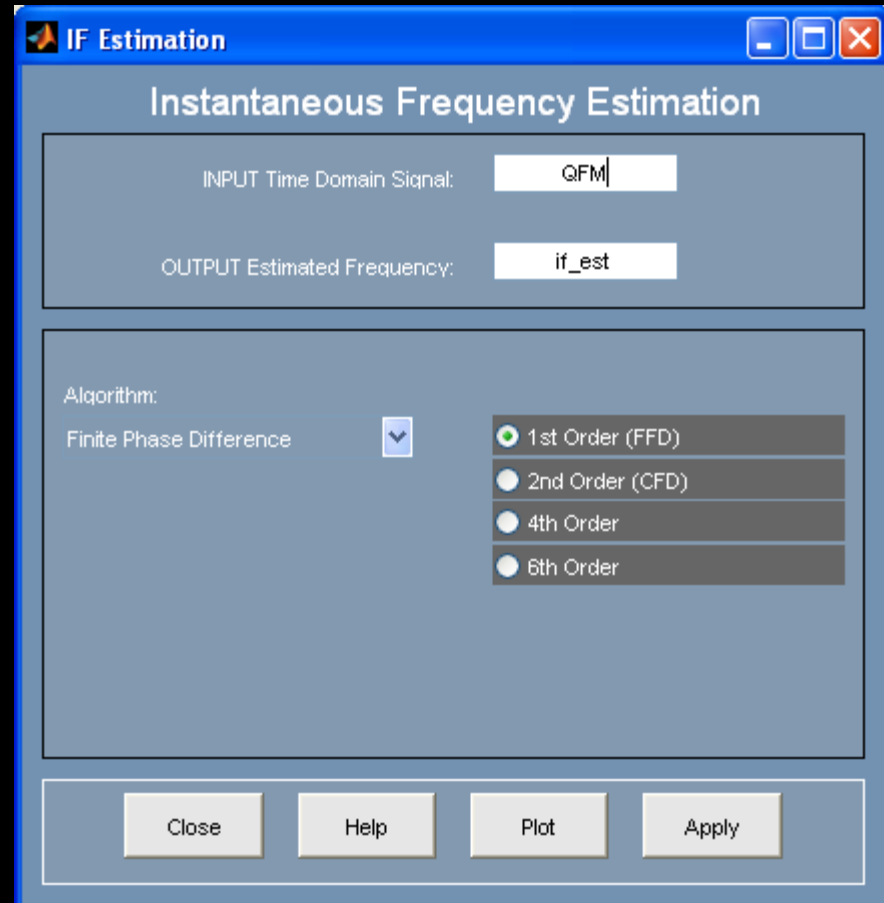
- Analytic signal can be used to directly estimate the IF of a signal (chapter 1)





$$IF(t) = \frac{1}{2\pi} \frac{d\phi(t)}{dt}$$

- The IF can also be estimated using several differentiation schemes, adaptive techniques, the peaks of a TFD, and zero crossings.

TFSA IF Estimation

Estimate the IF of
a quadratic FM in
the presence of
noise




 IF Estimation   

Instantaneous Frequency Estimation

INPUT Time Domain Signal:

OUTPUT Estimated Frequency:

Algorithm:

Finite Phase Difference 

☒ 1st Order (FFD)

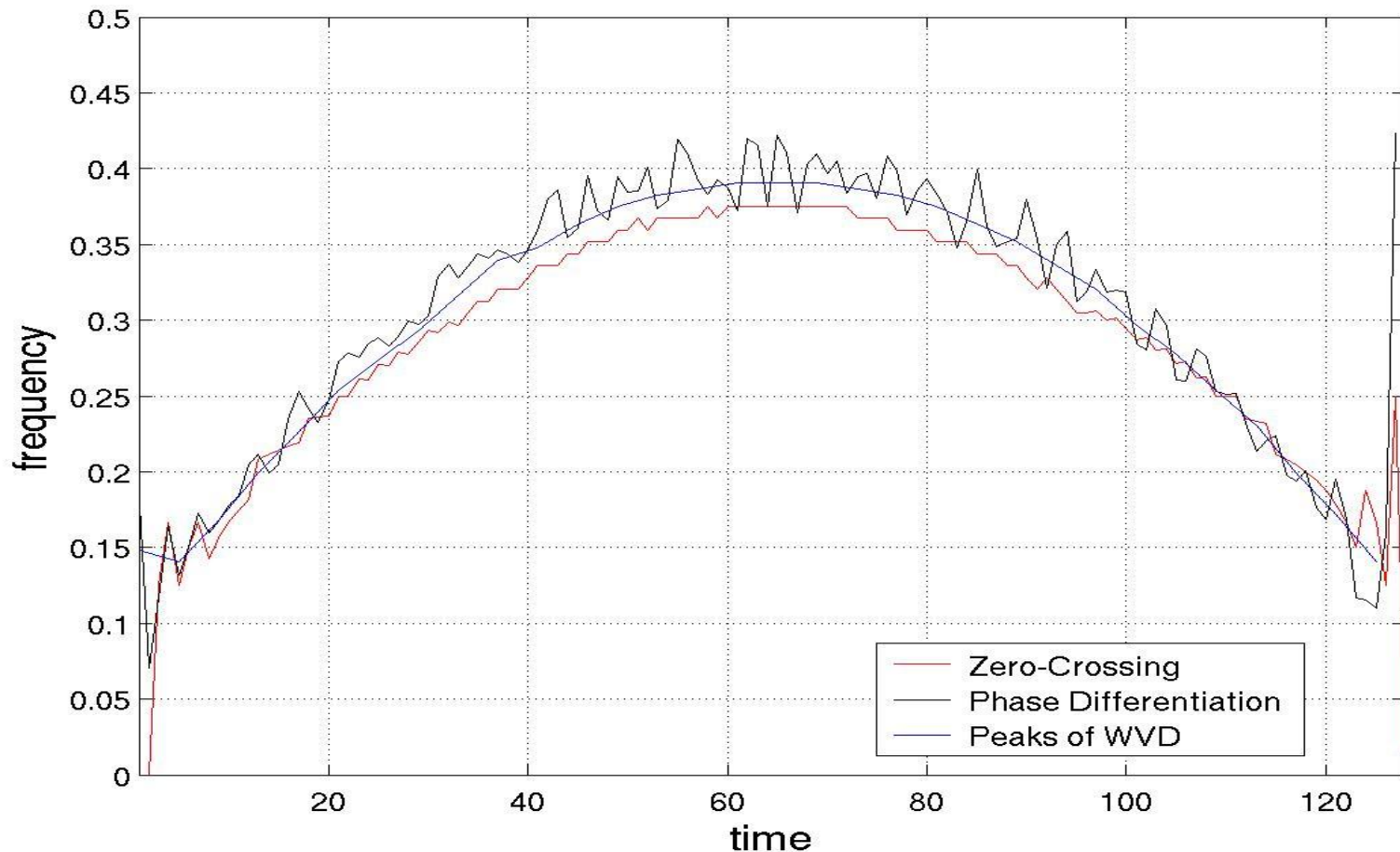
☐ 2nd Order (CFD)

☐ 4th Order

☐ 6th Order

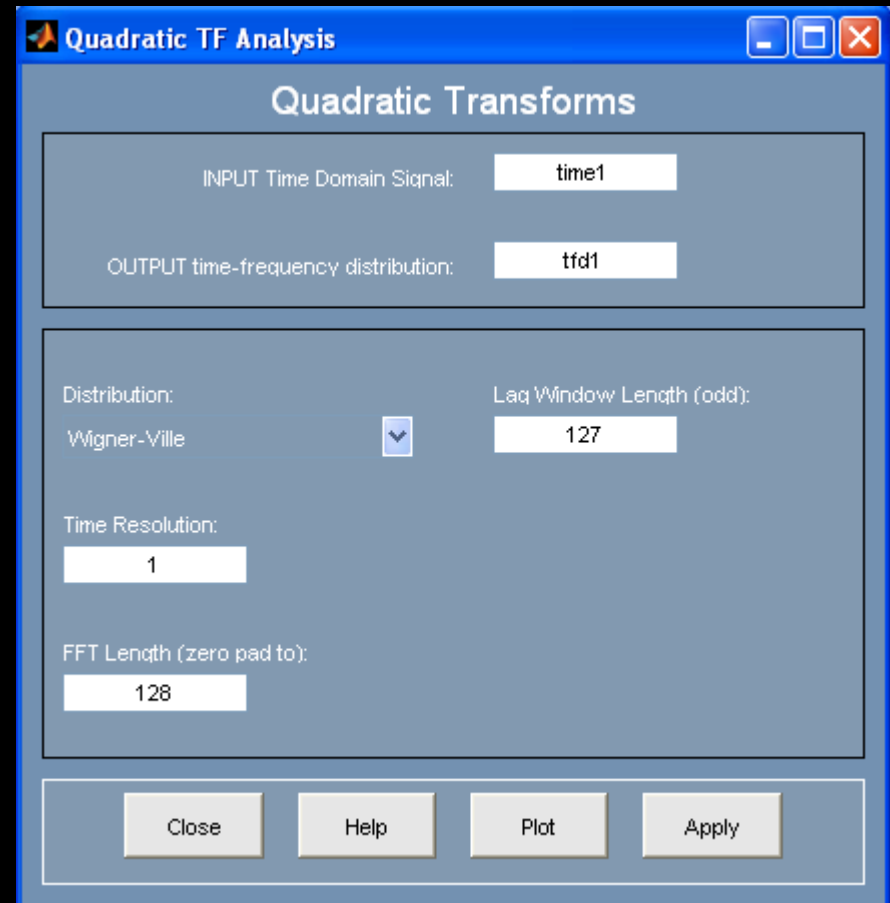
TFSA IF Estimation

```
>> plot(if_est1); hold; plot(if_est2,'r'); plot(if_est3)
```



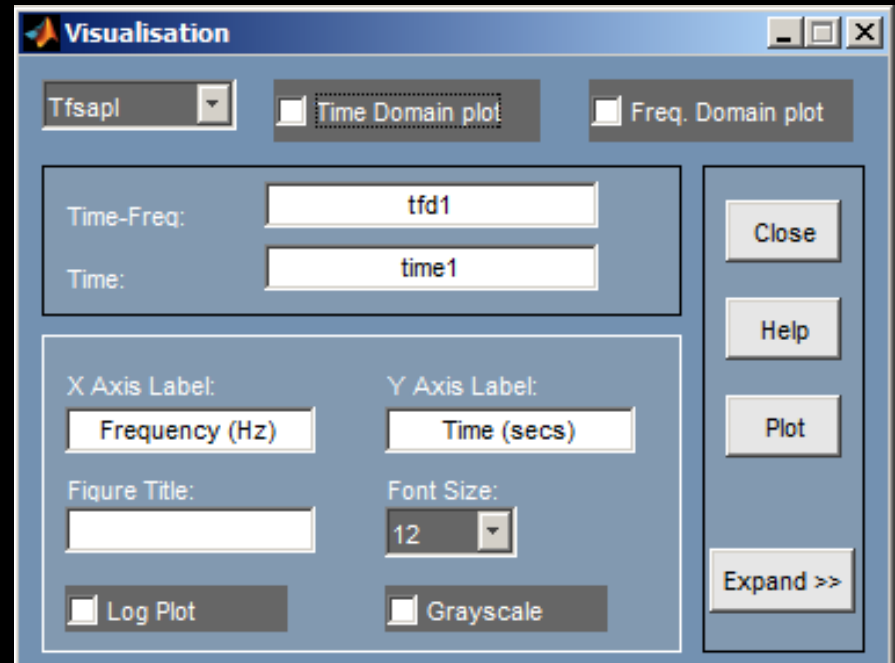
Quadratic TFDs

- Quadratic class of TFDs (Chapter 3, pp 59)
 - Wigner-Ville
 - Smoothed WVD
 - Spectrogram
 - B-distribution
 - Modified B-distribution
 - Ext Modified B-distribution
 - CKD
 - MDD
 - ...
- Cross WVD
- Ambiguity



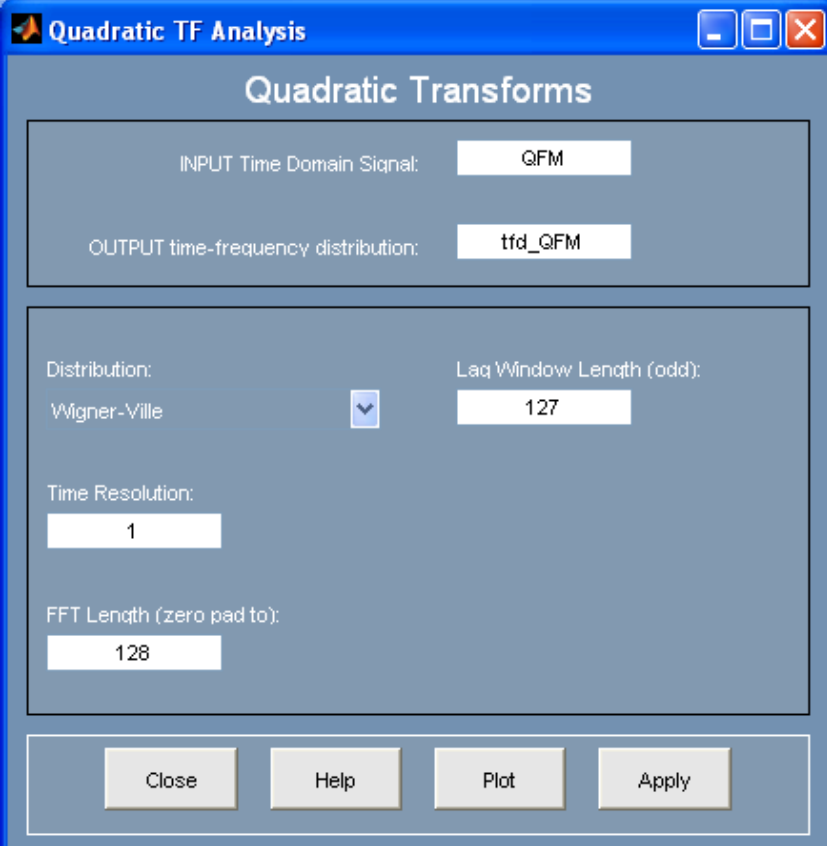
Visualisation

- Provides an array of visualisation options for the 3-D distribution (energy-time-frequency)
 - Specific TFD plot
 - Waterfall
 - Image
 - Logarithmic
 - Colormap




Quadratic TFD example

- Estimate the TFD of the quadratic FM signal.



The screenshot shows a software window titled "Quadratic TF Analysis". Inside, there is a section titled "Quadratic Transforms" with several input fields and buttons. The "INPUT Time Domain Signal" is set to "QFM". The "OUTPUT time-frequency distribution" is set to "tfd_QFM". The "Distribution" is set to "Wigner-Ville" with a dropdown arrow. The "Lag Window Length (odd)" is set to "127". The "Time Resolution" is set to "1". The "FFT Length (zero pad to)" is set to "128". At the bottom, there are four buttons: "Close", "Help", "Plot", and "Apply".

| Quadratic Transforms | |
|-------------------------------------|--------------|
| INPUT Time Domain Signal: | QFM |
| OUTPUT time-frequency distribution: | tfd_QFM |
| Distribution: | Wigner-Ville |
| Lag Window Length (odd): | 127 |
| Time Resolution: | 1 |
| FFT Length (zero pad to): | 128 |
| Close Help Plot Apply | |

 Quadratic TF Analysis

Quadratic Transforms

INPUT Time Domain Signal:


QFM

OUTPUT time-frequency distribution:

tfrep_b

Distribution:

B-distribution



Lag Window Length (odd):

15

Time Resolution:

1

Parameter Beta:

0.01

FFT Length (zero pad to):


128

Close

Help

Plot

Apply

 **Visualisation** Minimize Maximize Close

Tfsapl ▼ ☒ Time Domain plot ☒ Freq. Domain plot

Time-Freq:

Time:

X Axis Label:

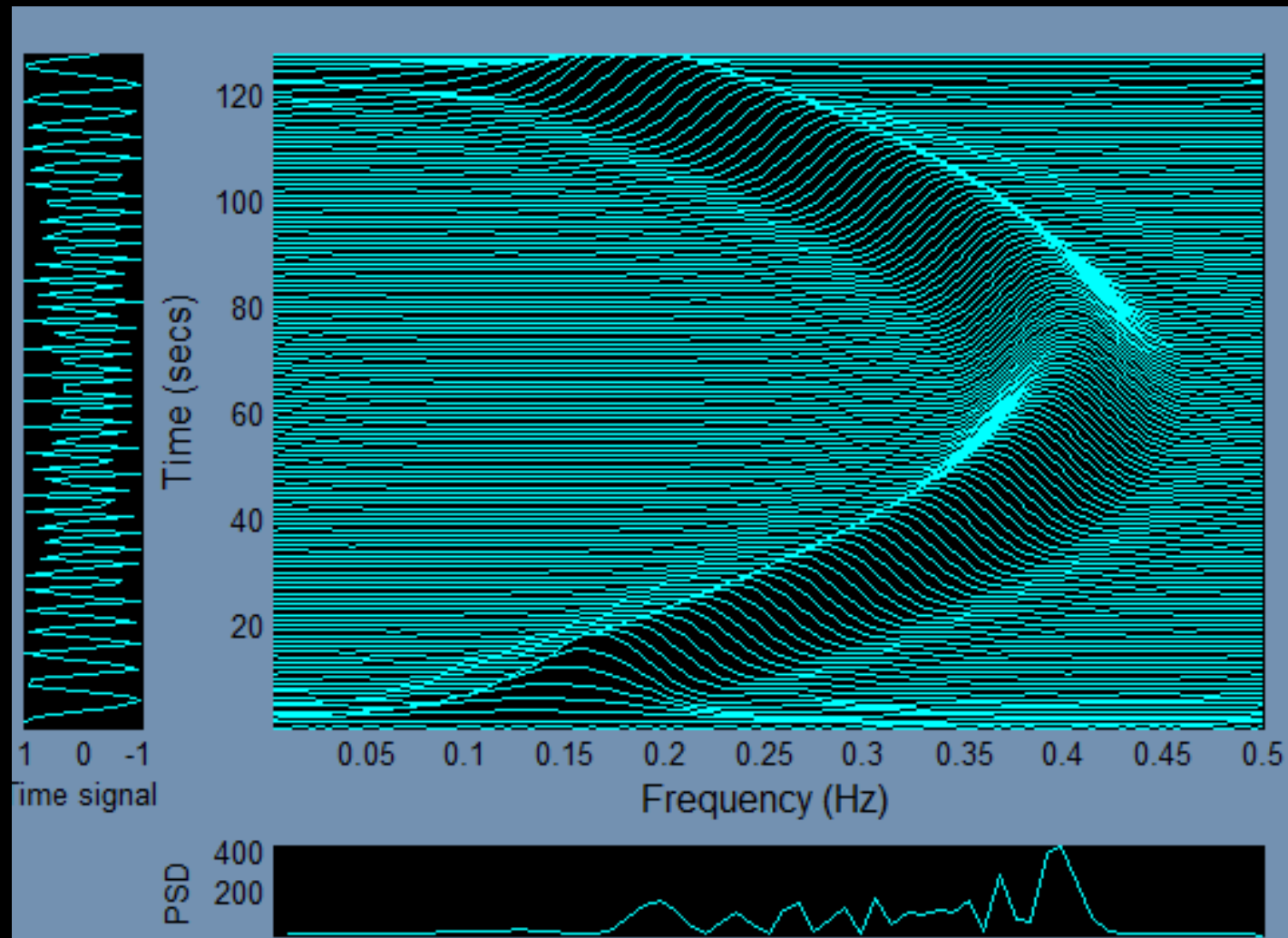
Y Axis Label:

Figure Title:

Font Size: ▼

☐ Log Plot ☐ Grayscale

Quadratic TFD example



Quadratic TFD example

- WVD

- win length = 15, nfft = 128, tres = 1

- Spectrogram

- win length = 15, nfft = 128, tres = 1, smooth win = 'hamm', smooth win length = 15

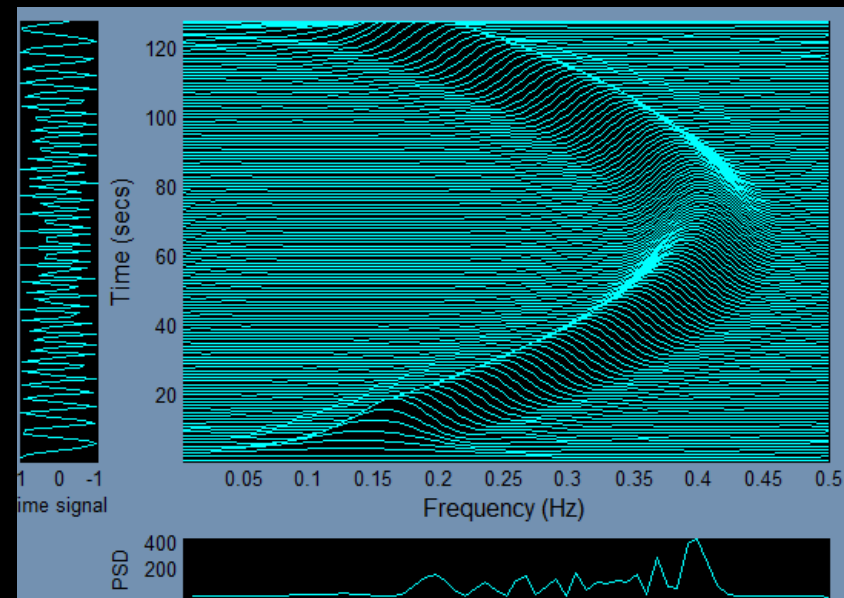
- Choi-Williams

- win length = 15, nfft = 128, tres = 1, sigma = 20

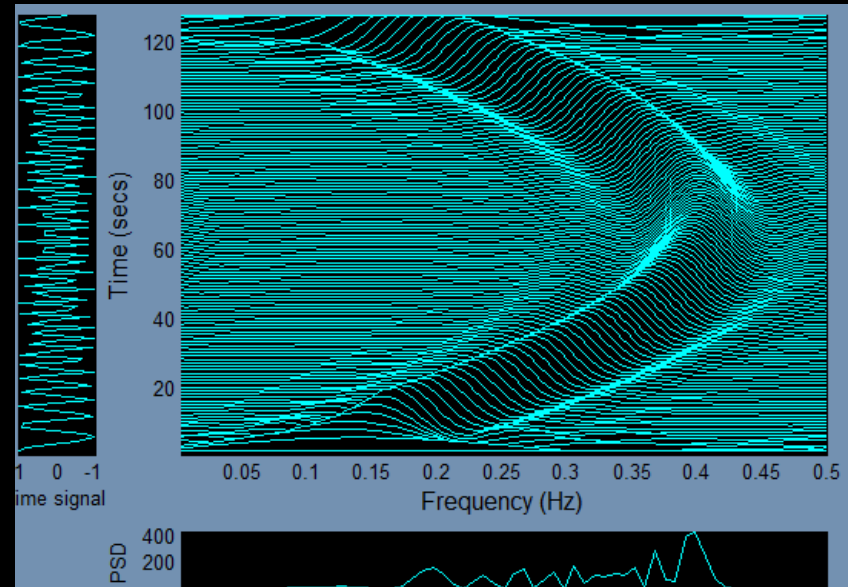
- B-distribution

- win length = 15, nfft = 128, tres = 1, beta = 0.01

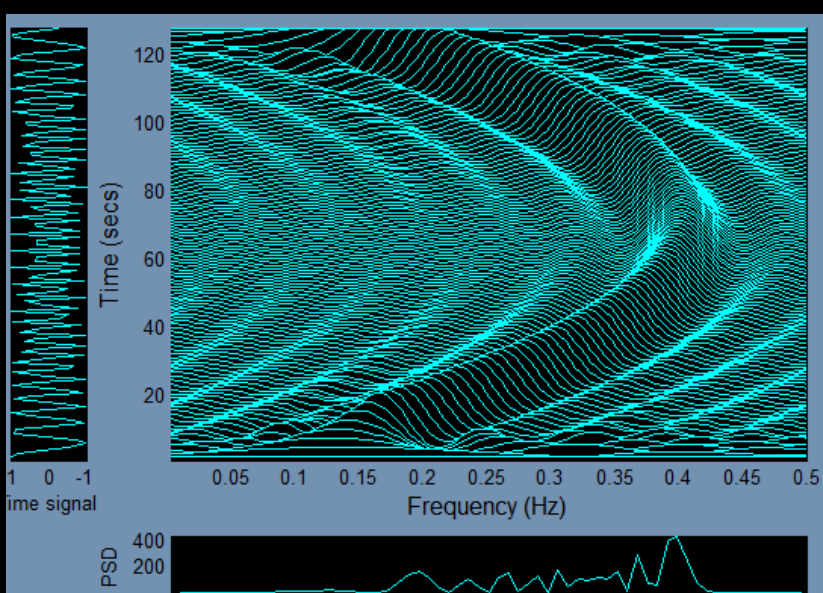
B-distribution



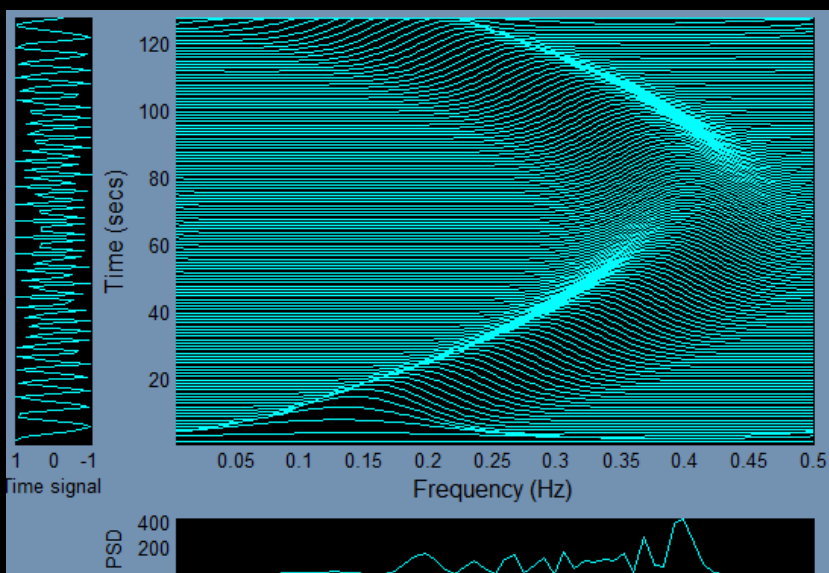
Choi-Williams



Wigner-Ville distribution

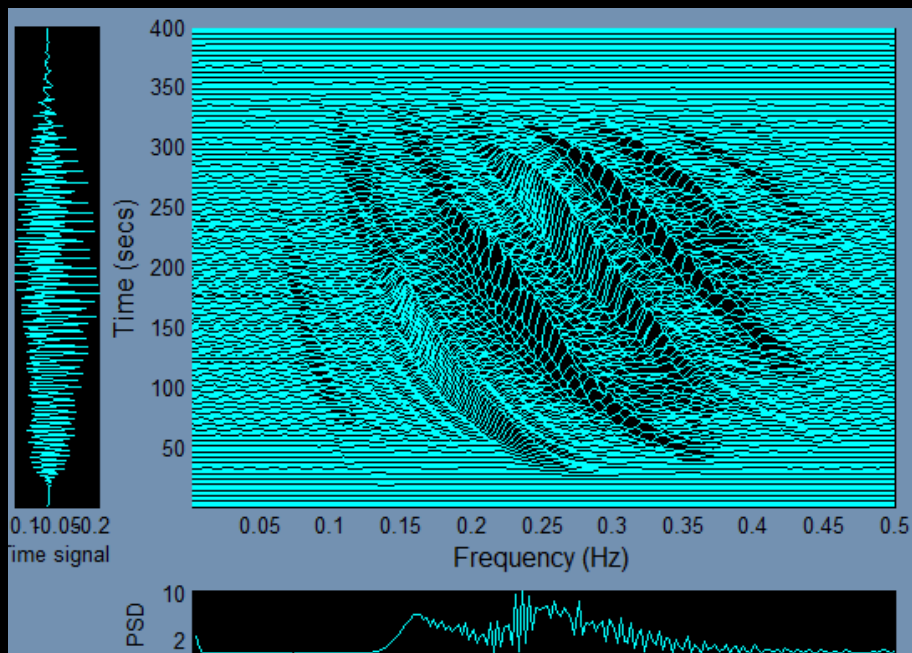


Spectrogram



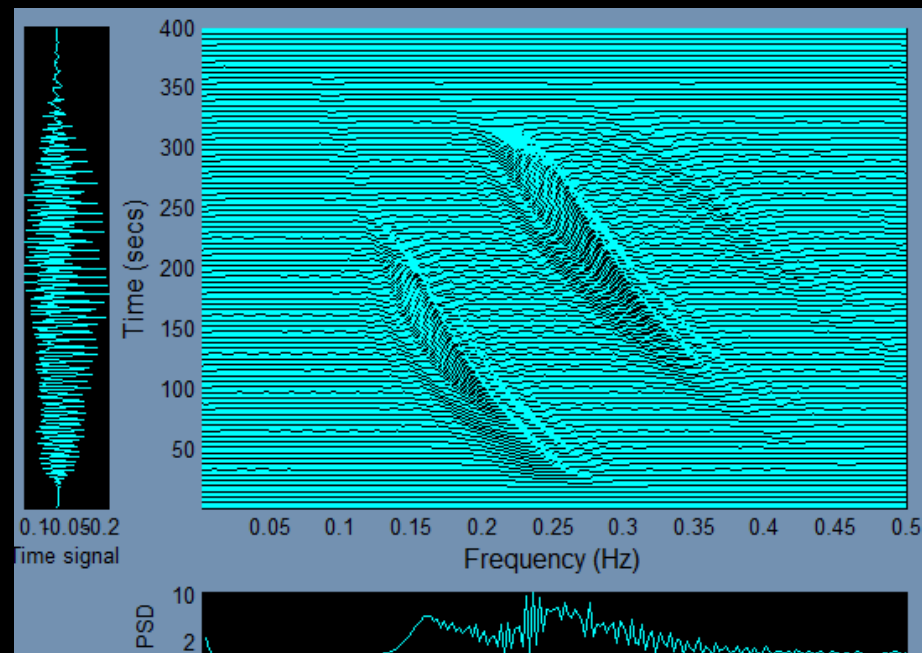
Quadratic TFDs Example

- Bat echolocation



Wigner-Ville distribution

win len = 63, nfft = 256,
tres = 2



Modified B-distribution


win len = 63, nfft = 256,
tres = 2, beta = 0.01

Signal Synthesis

- Signal Synthesis
 - STFT (overlap and add)
 - STFT (IDFT)
 - Modified STFT
 - Modified Spectrogram
 - WVD
- Time frequency filtering

Example

- Perform signal synthesis on a WVD of a linear FM signal
 - Generate LFM ($f_{\text{range}} = 0.1 - 0.4$, $\text{len} = 128$)
 - Find TFD using WVD ($\text{tres} = 1$, $\text{win len} = 127$)
 - Synthesise using WVD method
 - Find TFD of synthesised window

 **Signal Synthesis** [-] [] [X]

Signal Synthesis

INPUT Time Frequency Distribution:

OPTIONAL Original Time Domain signal:

OUTPUT Time Domain signal:

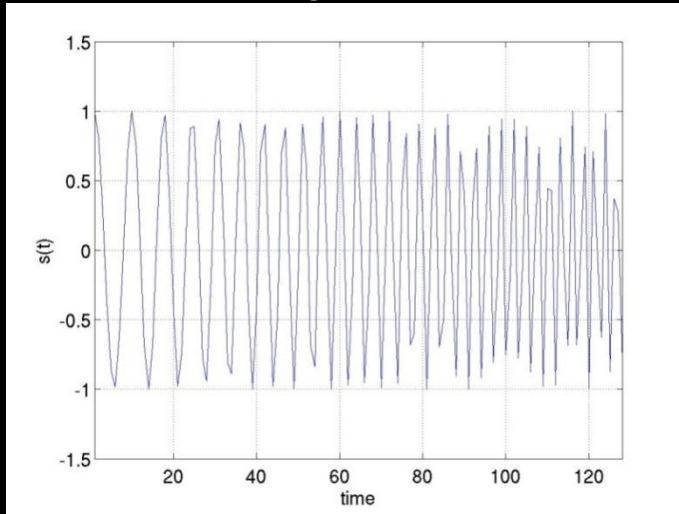
Distribution: ▼

Lag Window Length (odd):

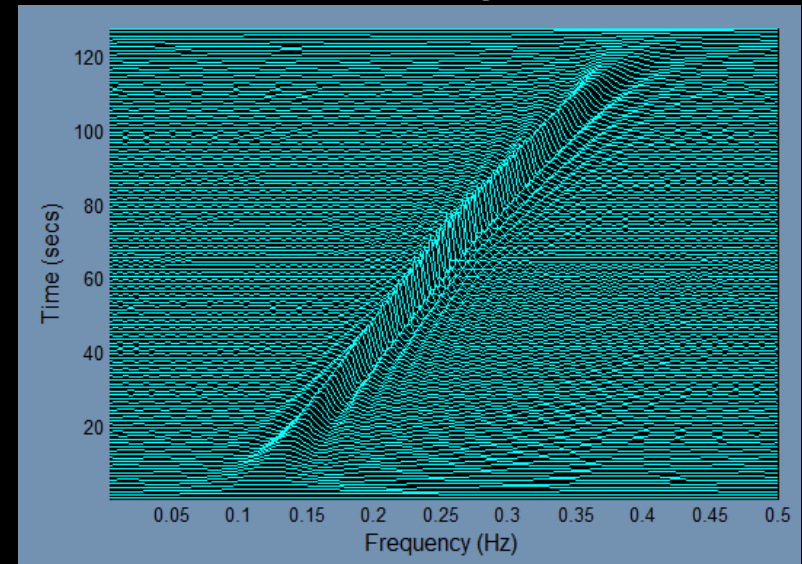
Original Signal to Reconstruct

☐ Supply Signal

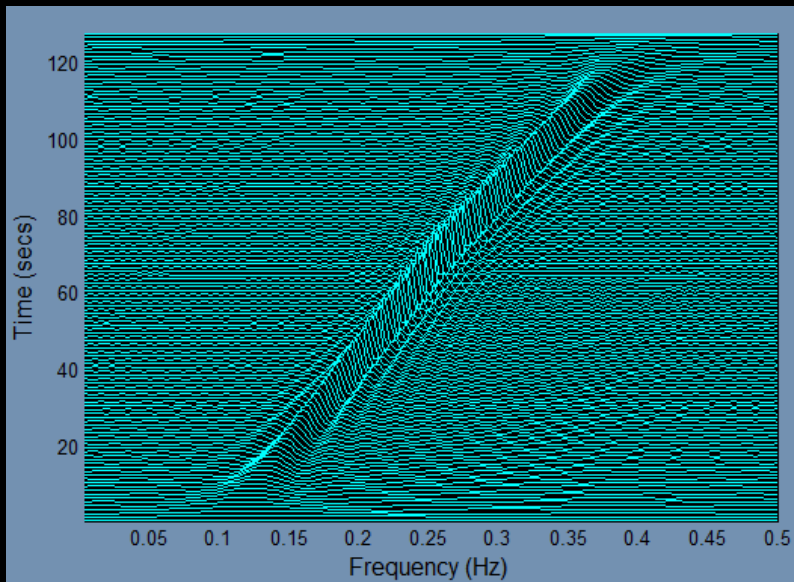
Signal



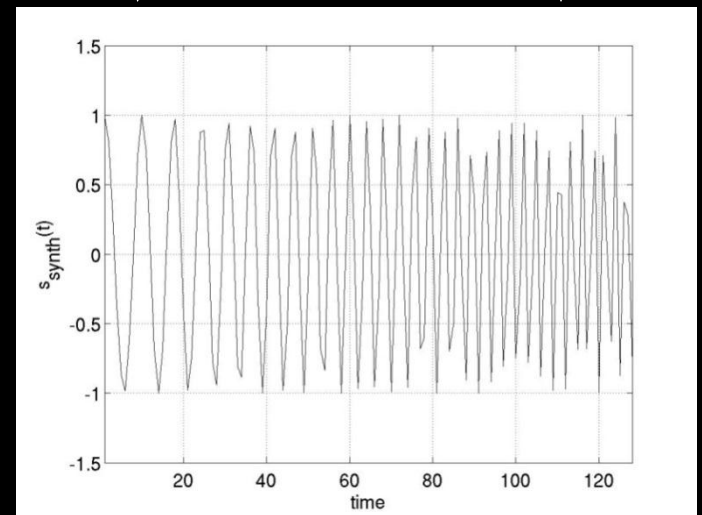
WVD of Signal



WVD of synthesised signal

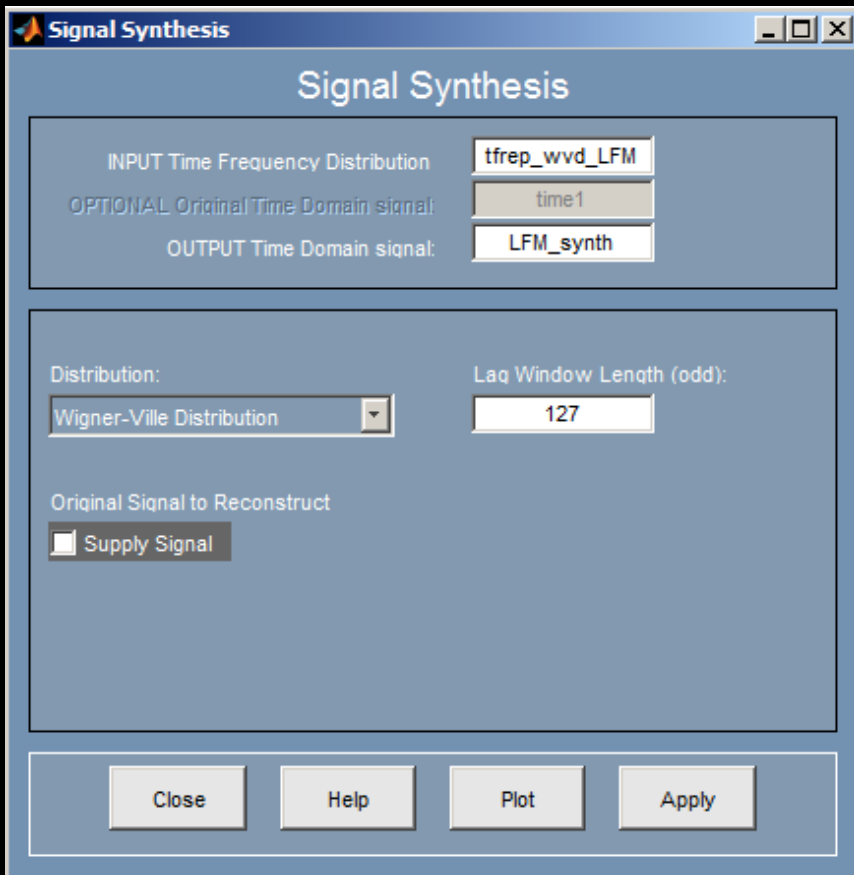


Synthesis

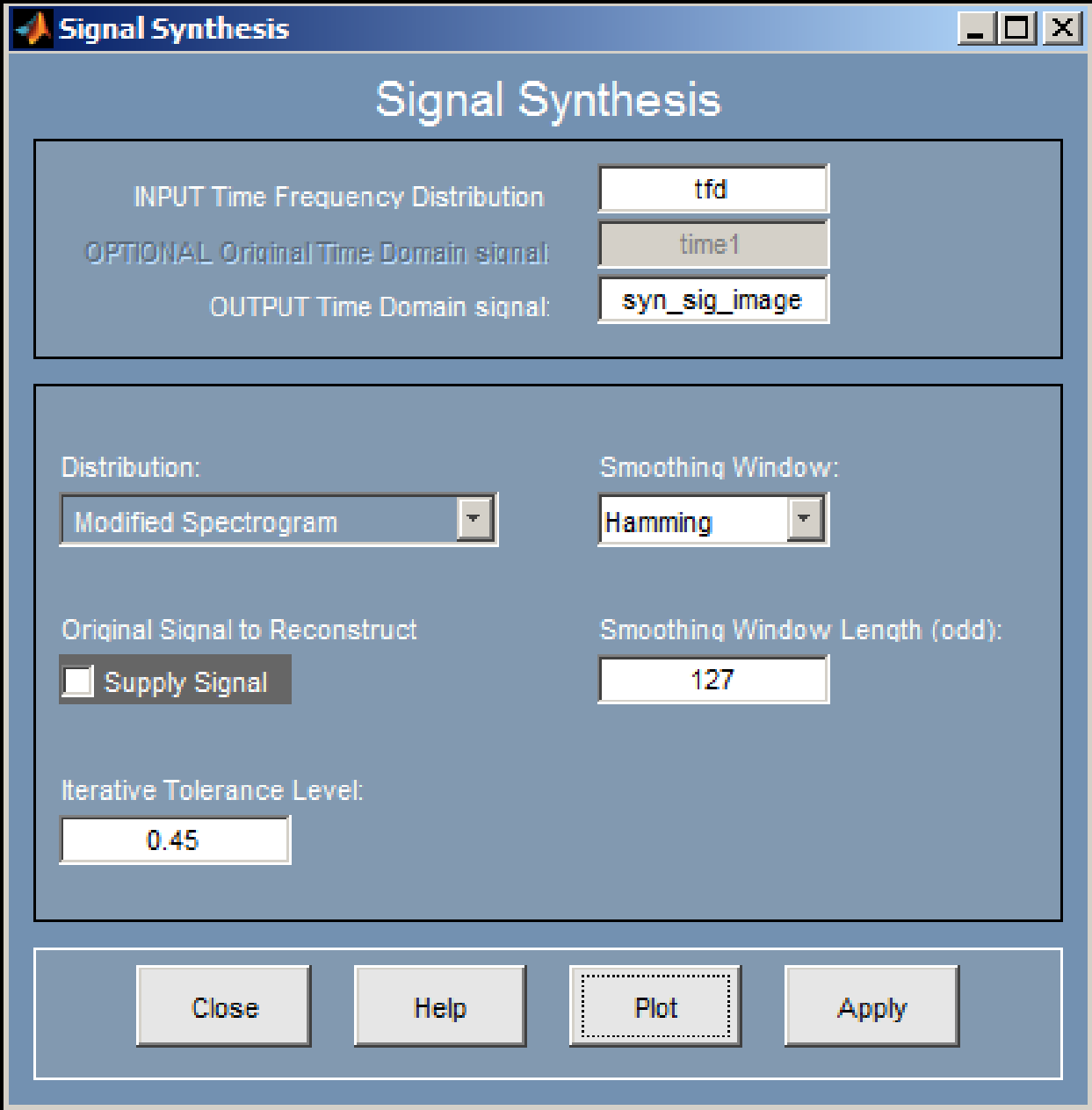


Signal Synthesis

```
>> tfd = double(rgb2gray(imread('signal1.jpg','jpg')));
```



TFD

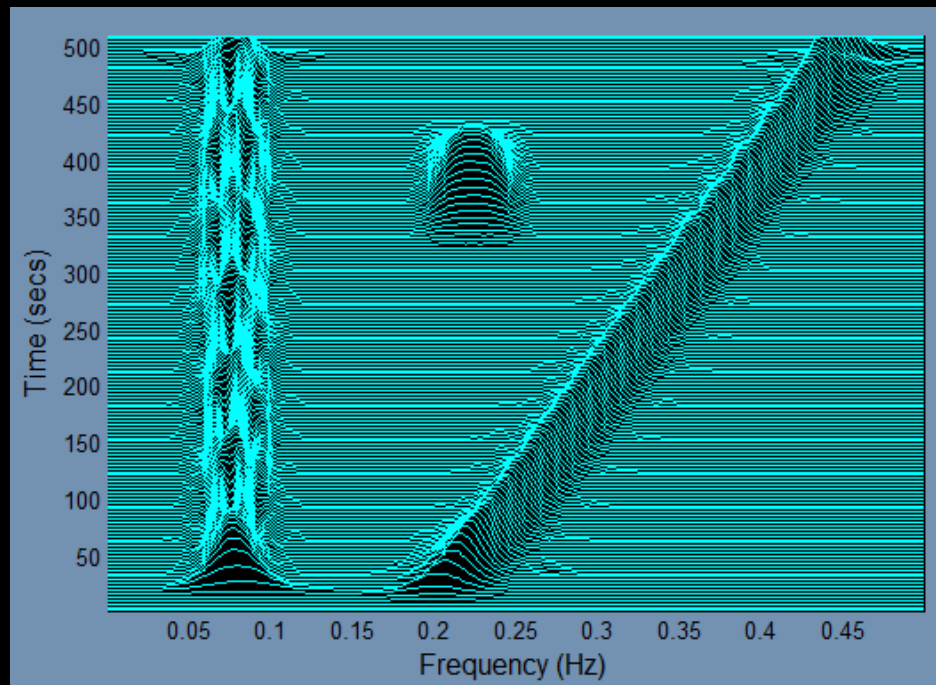


Signal Synthesis

Modified Spectrogram



Original TFD



Synthesised TFD

TFD generated using the spectrogram (win len = 127, tres = 3, smth win = 'hamm', smth win len = 127, nfft = 512)

Signal Synthesis

- Try for 'signal2.jpg' with the same parameters as the previous example

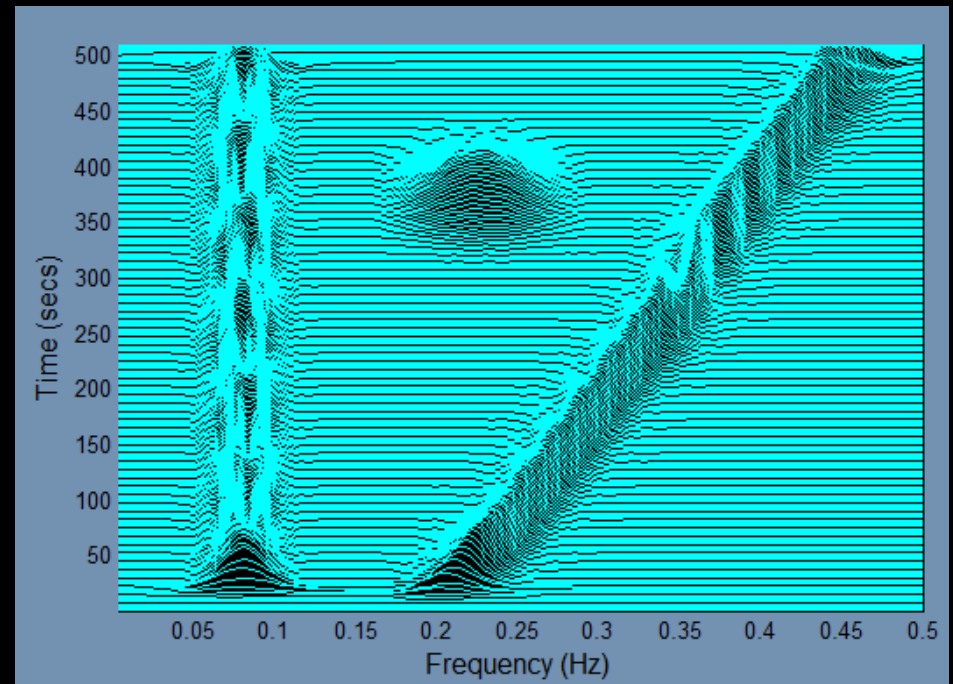
```
>> tfd =double(rgb2gray(imread('signal2.jpg','jpg')));
```

Signal Synthesis

Modified Spectrogram



TFD (signal2.jpg)



Synthesised TFD

Other tools

- Scale analysis
 - Wavelet Transform
 - Daubachies
- Toolbox Demo
- Higher Order TFDs
- Power Spectral Estimation
 - Periodogram