

# CHAPTER 23

## Solutions

### Exercise 1

TBC

### Exercise 2

Let the principal amount to be invested (in dollars) be  $N = 100$ .

The iTraxx XO follows the path  $\{330, 360, 320\}$ . The Libor rate is fixed at  $L_t = 5\%$ . The leverage ratio is  $\lambda = 2$ .

(a) The general strategy is to go through the following steps:

- Set  $V_{t_0} = N_{t_0} = 100$ . Calculate the floor

$$F_{t_0} = \frac{V_{t_0}}{(1 + r_t)^5} = \frac{100}{(1 + 0.05)^5} = 78.35$$

- The cushion is:

$$Cu_{t_0} = 100 - 78.35 = 21.65.$$

- Amount to be invested in risky asset is

$$R_{t_0} = \lambda \times Cu_{t_0} = 2 \times 21.65 = 43.30$$

which is the amount invested on iTraxx XO index. At the end of the year the spread received on the notional is  $3.3 \times R_{t_0} = 1.43$ . The balance  $D_{t_0} = 100 - 43.30 = 56.70$  is kept in a default-free deposit account enjoying Libor. At the end of the year the spread received on the notional is  $3.3 \times R_{t_0} = 1.43$ .

- As the crossover index changes over time  $t_1, t_2, \dots$ , the positions on iTraxx XO and default-free bond investments are changed so as to keep the leverage ratio constant.

(b)

### Period 1

$$\text{Calculate } V_{t_1} = 100 \times (1 + L_{t_0}) + R_{t_0} \times c_{t_0} = 105 + 43.30 \times 0.033 = 106.43.$$

Now

$$F_{t_1} = \frac{100}{1.05^4} = 82.27.$$

Thus, the new

$$R_{t_1} = 2 \times (V_{t_1} - F_{t_1}) = 2 \times 24.16 = 48.32.$$

### Period 2

Calculate

$$\begin{aligned} V_{t_2} &= V_{t_1} \times (1 + L_{t_0}) + R_{t_1} \times c_{t_1} \\ &= 111.75 + 48.32 \times (0.036) = 113.49. \end{aligned}$$

Hence

$$F_{t_2} = \frac{100}{1.05^3} = 86.38.$$

Thus, the new

$$R_{t_2} = 2 \times (V_{t_2} - F_{t_2}) = 2 \times 27.11 = 54.22.$$

### Period 3

Calculate

$$\begin{aligned} V_{t_3} &= V_{t_2} \times (1 + L_{t_0}) + R_{t_2} \times c_{t_2} \\ &= 119.16 + 54.22 \times 0.032 = 120.90. \end{aligned}$$

Here

$$F_{t_3} = \frac{100}{1.05^2} = 90.70.$$

Thus, the new

$$R_{t_3} = 2 \times (V_{t_3} - F_{t_3}) = 2 \times 30.200 = 60.40.$$

(c) Now there is a default and the index is  $c_{t_3} = 370$ . The notional investment iTraxx XO was 53.30 which becomes  $53.40 \times 29/30$ . An amount of  $60.40/30$  has to be paid, but with recovery rate 40%,  $60.40/30 \times 0.40$  is recovered. Hence

$$V_{t_4} = V_{t_3} \times (1 + L_{t_0}) + \frac{R_{t_2}}{30} \times (1 - 0.4) \times R_{t_2} \times c_{t_3}$$

$$= 120.90 \times (1.05) - 60.40/30 \times (1 - 0.4) + 60.40 \times 29/30 \times 0.037 = 127.90.$$

$$F_{t_4} = \frac{100}{1.05} = 95.24.$$

Thus, the new

$$R_{t_4} = 2 \times (V_{t_4} - F_{t_4}) = 2 \times 32.68 = 65.36$$